OpenMI coupling of FEFLOW and MIKE SHE

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Abstract

Effective environmental management requires integrated modelling not only of catchment processes but their interactions. The motivation of this study was to combine the strengths of FEFLOW and MIKE SHE to improve our ability to solve complex problems in water resources and environmental management. This is achieved by coupling the two models using OpenMI technology. OpenMI is a standard which allows different modelling tools to exchange data dynamically during the simulation. One advantage of such a coupling is that the comprehensive surface and unsaturated zone processes in MIKE SHE can be combined with the advanced subsurface modelling in FEFLOW. This represents a very challenging coupling problem as both models are individually quite complex; FEFLOW is based on the finite-element method and can handle quadrilateral or unstructured triangular meshes, while the finite-difference based MIKE SHE employs a regular (Cartesian) grid. The proposed coupling requires exchange of data between one-dimensional, two-dimensional and three-dimensional fields. This paper briefly describes how the coupling of these two models is achieved. Systematic tests of the coupled modelling tools have been carried out in order to verify the coupling of different components of FEFLOW and MIKE SHE. Selected cases involving different combinations of processes within the coupling such as river flows, unsaturated flows, drainage and extractions are examined against existing analytical and numerical solutions. The results presented here demonstrate that the two models have been successfully coupled. The resulting coupled model provides the capability to treat a number of interesting new applications that combine the strengths of both models. For example, future work will include combining coarse scale surface modelling with high-resolution modelling of groundwater within a large-scale catchment, and coupling of overland and unsaturated flow processes with seawater intrusion in coastal aquifers which can in turn be used to examine the impacts of climate change.

1. INTRODUCTION

Proper understanding of the hydrological cycle in nature is needed for the effective management of water resources. Numerous studies have been carried out to analyse individual components of the cycle and modelling tools have been developed to achieve this. Traditionally different hydrological processes such as surface water and groundwater have been managed and modelled separately in part due to the complexity of the real hydrological systems and limitations in computational resources. However in reality not only are the details of each process important but also the mutual interactions between the different processes are often crucial to our understanding of the water cycle. Surface water and groundwater interactions affect a number of water management issues such as conjunctive water use for water supply and irrigation, the transformation of nutrients, wetland dynamics and ecology, flooding behaviour, bio-geochemical conditions in riparian areas, stream temperature, etc. Groundwater resources often have a complex dependency with adjacent water courses, wetlands and stream networks. Groundwater is, on the other hand, an important factor in freshwater wetlands and in controlling low flows and maintaining environmental flows. This need to manage, at the catchment scale, both surface water and groundwater and the associated freshwater ecosystems is embodied, for example, in the requirements of the EU Water Framework. Therefore, a more comprehensive and holistic modelling approach is required to solve many of today's complex water management problems. For example, assessing the impact of climate change or land use change on sustainability of a coastal aquifer system may require integrated modelling of the surface water resources, the aquifer and their interaction.

There are a growing number of surface water-groundwater models. However each model has its own strengths and weaknesses, for example there are relatively few that include river management capabilities (Valerio et al., 2010). The motivation of this study is to combine the strengths of two comprehensive water resources models, MIKE SHE and FEFLOW to address more complex environmental problems. In this study, we aim to achieve this by coupling MIKE SHE and FEFLOW using OpenMI technology. Linking existing models provides a cost-effective and powerful method for expanding integrated modelling capabilities. This paper demonstrates how this approach is being used to enhance the process modelling capabilities of both tools. There are however a number of important challenges in successfully integrating different process descriptions using different models. These include matching the temporal and spatial scales of the different processes, modelling subgrid processes, ensuring fast, accurate and stable numerical solutions and properly accounting for the effects of coupling between the processes.

MIKE SHE is a fully distributed, process-based hydrological model and includes process models for evapotranspiration, overland flow, unsaturated flow, groundwater flow, and channel flow and their interactions including solute transport (Abbott et al., 1986a&b; Refsgaard and Storm, 1995). Fully distributed means that the model can represent spatial variations in surface hydrological parameters such as soil and vegetation type, in subsurface parameters such as geological layering and lenses, together spatial variations in the boundary conditions such rainfall and potential evapotranspiration or groundwater pumping and surface irrigation. Model input is data-driven in the sense that these spatial variations can be specified independently of the simulation resolution. Each of these processes is described either by an appropriate physics-based governing equation or by a simpler conceptual representation and a user can tailor the model structure by choosing processes to be included and solution methods (Butts et al., 2004). MIKE SHE is therefore a comprehensive catchment modelling framework with applications ranging from aquifer management and remediation to wetland management, flooding and flood forecasting (Graham and Butts, 2006; Butts & Graham, 2008). MIKE SHE is dynamically coupled to MIKE 11, which is a one-dimensional surface water model that simulates fully dynamic channel flows and is therefore able to represent river processes and river management (Butts et al., 2004; Thompson et al., 2004). While the process-based approach allows different model structures to be applied within the same modelling framework, in the original concept the different flow processes are described by the governing partial differential equations and these are then solved by discrete numerical approximations in space and time using finite differences.

FEFLOW is an advanced subsurface water modelling system for modelling fluid flow and transport of dissolved constituents and/or heat transport processes in the subsurface including density dependent flow (Diersch and Kolditz, 1998; Kolditz et al., 1998; Diersch, 2001; Trefry and Muffels, 2007; DHI-WASY, 2010) FEFLOW is highly flexible finite element model for subsurface flow and transport and more recently interactions with river systems (Monninkhoff and Li, 2009). The advantage of the finite element approach is the flexibility to represent complex geologies with a high spatial resolution, including sloping layers and anisotropy and the ability to precisely represent features like rivers, fractures, tunnels and well locations. One of the other key strengths of FEFLOW is the number of advanced descriptions of subsurface processes such as variably saturated and density dependent flow, saltwater intrusion, multi species chemistry and transport and heat transport. Applications of FEFLOW include: regional groundwater management, saltwater intrusion, seepage through dams and levees, mine water management, groundwater management in construction and tunnelling projects, land use and climate change scenarios, groundwater remediation and natural attenuation, geothermal energy and groundwater-surface water interactions.

The main reasons for coupling MIKE SHE and FEFLOW are

- the powerful subsurface modelling capabilities of FEFLOW, especially grid refinement, three dimensional unsaturated flow and variable density flow including saltwater intrusion would be available in MIKE SHE

- the surface process capabilities in MIKE SHE particularly the ability to calculate dynamically recharge to groundwater directly from precipitation and potential evapotranspiration and subsequently determine both groundwater flow and river discharge, would be available in FEFLOW

The exchange of data needed to couple FEFLOW and MIKE SHE is performed using the OpenMI protocol. The Open Modelling Interface and Environment (OpenMI) is a set of standardized interfaces and classes that have been developed by OpenMI Association (www.openmi.org), and partly funded by EU through the 5th framework project, HarmonIT, and the LIFE Programme, OpenMI-LIFE. OpenMI allows the models to communicate at run-time, across differences in time step, and spatial resolution, and discretization although in this case the meteorological and hydrological models use the same surface grid size. OpenMI was developed in an attempt to provide a widely accepted unified method designed to simplify linking of hydrology-related models, both legacy codes and new ones, (Gregersen et al., 2005, 2007). It is based on direct access of the model at run-time, not using files for data exchange. To achieve a dynamic coupling both models were made OpenMI compliant by developing the appropriate interfaces. These interfaces allow for run-time and time step control to an outside entity and provide access to internal state variables and parameters.

In this study we briefly describe the approach used in coupling MIKE SHE and FEFLOW using OpenMI. This represents quite a challenging coupling problem as it contains both one-dimensional, two dimensional and three-dimensional elements. In addition, the coupling must match the block-centred finite difference solutions from MIKE SHE with the variable mesh finite element solutions from FEFLOW. The performance of this coupled model is then demonstrated and evaluated against both analytical and numerical solutions for a number of verification cases involving both surface water and groundwater components. The resulting coupled model provides the capability to treat a number of interesting new applications that combine the strengths of both models. For example, future work will include combining coarse scale surface modelling with high-resolution modelling of groundwater within a large-scale catchment, and coupling of overland and unsaturated flow processes with seawater intrusion in coastal aquifers which can in turn be used to examine the impacts of climate change.

2. COUPLING METHODOLOGY

In this study, the groundwater system is modelled by FEFLOW and surface water and unsaturated zone were modelled by MIKE SHE. While FEFLOW has the option to represent the unsaturated zone using the three-dimensional Richards equation, in many cases the unsaturated flow is predominantly vertical. Therefore the one-dimensional solution used in MIKE SHE is often sufficient and expected to save computation time particularly for large-scale catchment modelling. MIKE SHE also has detailed descriptions of the evapotranspiration and recharge processes. Although these are not completely represented in the test cases presented here, these are important processes to represent in the management of water resources at the catchment scale.

The two models exchange recharge to the top aquifer and hydraulic head in each computational layer of aquifer. MIKE SHE calculates the recharge entering the aquifer which is passed to FEFLOW as a source term and the drainage to the river system which is passed to FEFLOW as a sink term. MIKE SHE calculates the exchange flows between the aquifer and river, based on the differences in head between the river and groundwater in MIKE SHE. These exchange flows are also passed to as a source/sink term. FEFLOW performs the calculation of the groundwater heads in each of the computational layers which are then returned to MIKE SHE. The new groundwater heads are then used by MIKE SHE in the next time step to calculate the recharge, drainage and exchange flows between the aquifer and the river. These exchange calculations are therefore explicit and may require careful choice of time step. While in simple cases it is possible to carry out this exchange for a single groundwater computational layer, in more general cases the entire three-dimensional groundwater head field calculated by FEFLOW must be passed to MIKE SHE. This means the MIKE SHE model must contain an identical set computational layers in its groundwater component and more generally that the models need to be specifically set up for coupling.

In order to couple two independent simulations, a time buffering adaptor within OpenMI is applied to take care of temporal interpolation when time steps in the two models are different. The differences in spatial discretization of two models are also managed in OpenMI. The computational mesh in MIKE

SHE is always a uniform, block-centred, finite difference grid while the FEFLOW mesh can be either quadrilateral or triangular elements with variable element size.

3. VERIFICATION STUDY

A series of test cases have been analysed in order to verify the coupled modelling tool. The tests were designed to test the transient behaviour of the coupling, matching of the finite difference and finite element meshes, particular components of the coupling as well as model performance and accuracy.

3.1. Case 1: Transient stream depletion (Hunt, 1999)

Hunt (1999) presented an analytical solution for the transient drawdown due to constant pumping in an infinite uniform aquifer bounded by constant head on one side and by a stream boundary. Figure 1 shows the problem considered by Hunt. This problem can be modelled using either MIKE SHE or FEFLOW or the coupled MIKE SHE-FEFLOW model. This provides a verification of the transient behaviour of the coupling and interaction between groundwater and the river model.

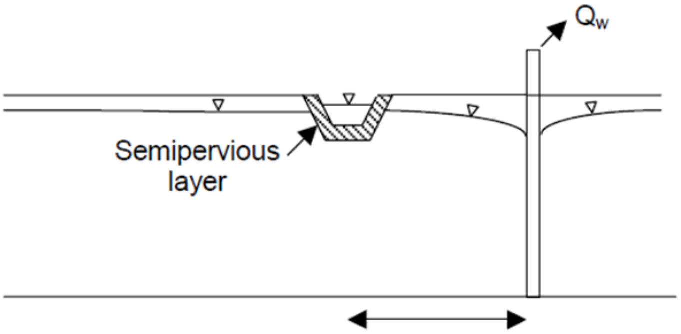


Figure 1 Schematic of the stream depletion problem considered by Hunt (1999)

Table 1 Model parameters for the stream depletion verification case

Shortest distance from the stream to the pumping well	95 m
Pumping rate	3.17 x 10^{-4} $m^{3/}s$
Thickness of the aquifer	10 m
Transmissibility of the aquifer	0.001 m^2/s
Storage coefficient of the aquifer	0.2
Stream bed leakage coefficient	1 x 10^{-5} m/s
Initial hydraulic head	10 m
Recharge	0 m^3/s

The model parameters used for the stream depletion case are presented in Table 1. The model domain is 1000 m by 1000 m which is large enough to compare the simulated water movement around the pumping well with the analytical solution based on the infinite aquifer assumption. A single computational layer was used to represent the aquifer in this case.

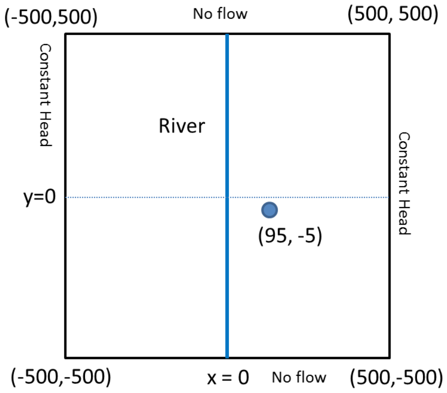


Figure 2 Horizontal view of model domain used for stream depletion

The aquifer boundaries are constant head on the left and right edges and no flow at the top and bottom edges, Figure 2. To represent the stream, we introduced a MIKE 11 model with a simple straight river located at x = 0. The river has symmetric artificial cross-sections which has 10m width at the levees level 11m and 5m width at the riverbed level 9.5m. The initial water depth and boundary water depth are fixed as 0.5m. The MIKE SHE setup used 10m by 10m grid (10000 grid cells). In order to investigate the impact of FEFLOW spatial resolution, two meshes were generated for FEFLOW; a coarse mesh (3263 elements) and fine mesh (29944 elements).

The simulated drawdown of groundwater and the analytical solution are compared in Figure 3. The transient behaviour is shown for the first 23 days after the onset of pumping for a well located directly between the pumping well and the river, 50 m from the well. Figure 4 shows the analytical drawdown and the simulated drawdown after 23 days along the cross-section through the well perpendicular to the river. These figures compare the analytical solution with the results obtained using MIKE SHE and with simulations using the coupling of FEFLOW and MIKE SHE. The simulated results match the analytical solution very well in all cases. The same accuracy could be achieved using the coarse mesh by using grid refinement around the well and the stream. This illustrates one of the powerful features of FEFLOW’s finite element formulation. At the same time detail describing the drawdown near the well can be obtained, Figure 4.

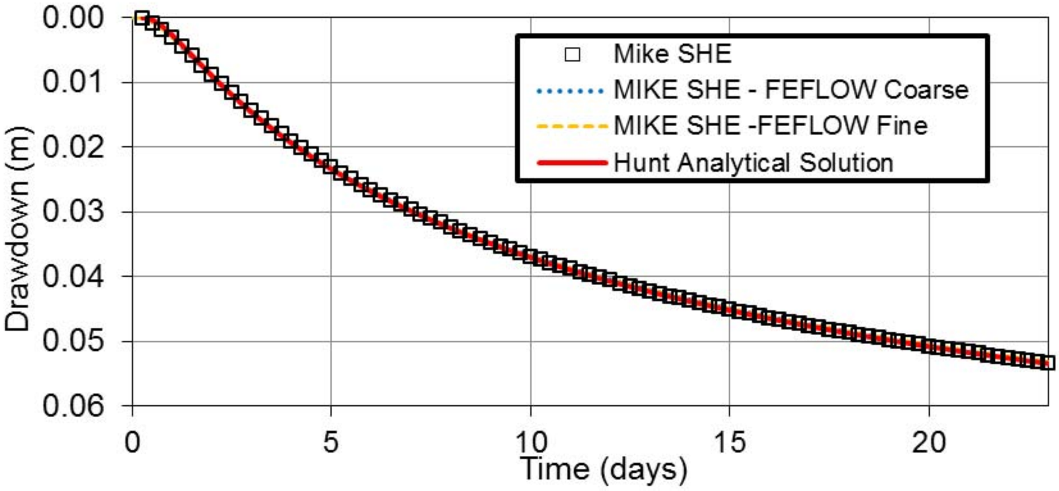


Figure 3 Comparison of the analytical drawdown by Hunt and the simulated drawdown by MIKE SHE and the MIKE SHE- FEFLOW coupled model. The results are obtained at a point along the line through the pumping well perpendicular to the river, 50 m away from the well.

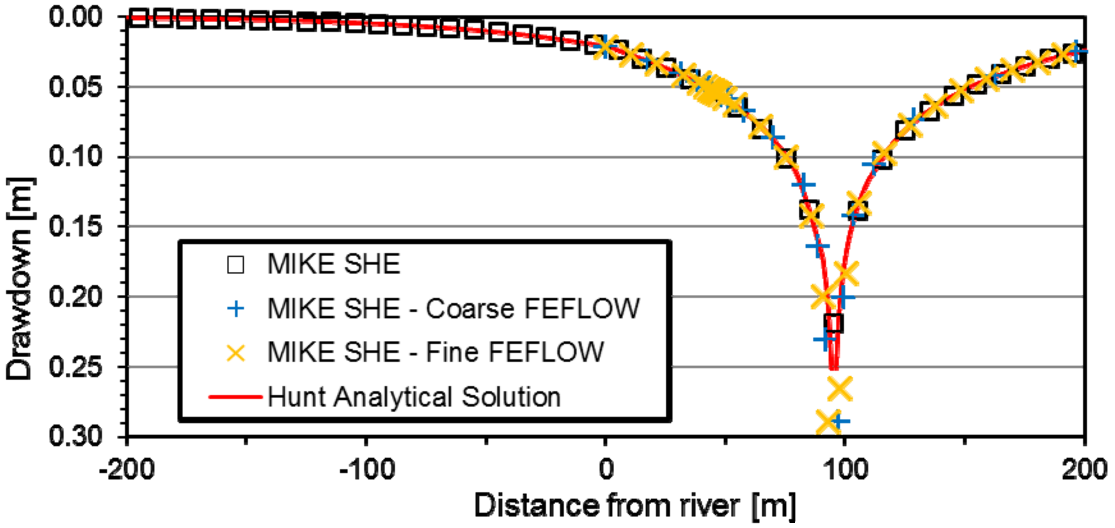


Figure 4 Comparison of the analytical drawdown by Hunt (1999) and the simulated drawdown in MIKE SHE and MIKE SHE- FEFLOW coupled model, perpendicular to the river and through the well after 23 days of pumping.

3.2. Case 2: Transient stream depletion with unsaturated flow

The stream depletion model set-up was then modified in order to verify the coupled model when including unsaturated flow and multiple layers, Figure 5. The geometry is similar but not identical to the first case and the pumping rate is increased to 0.003 m^3/s. A single soil type is used in the unsaturated zone. The soil properties are shown in Figure 6 and correspond to a fine sand. Initially, the rainfall and recharge is zero, then after 13 days a constant rainfall of 2.4 mm/day is applied over the next 5 days.

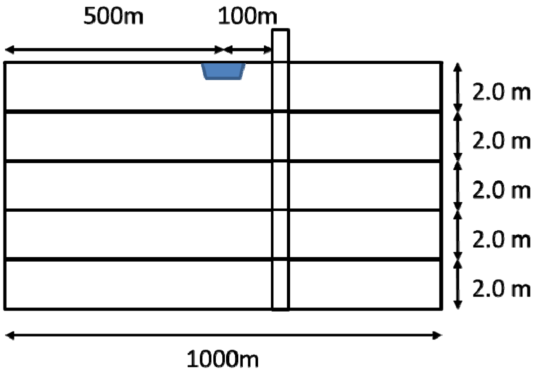


Figure 5 Modified stream depletion model including unsaturated flow and multiple layers.

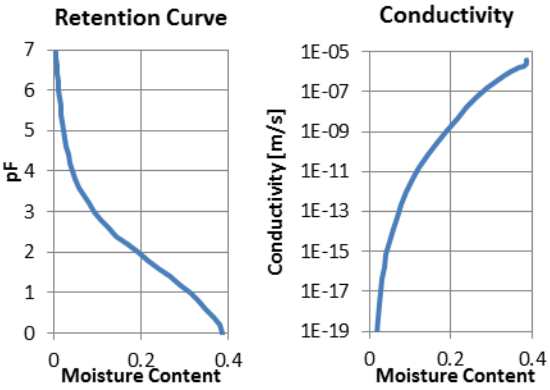
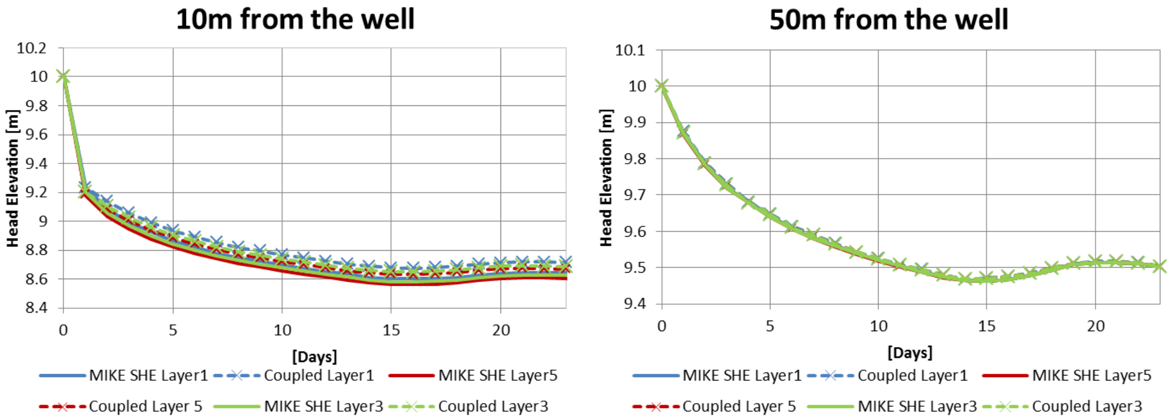


Figure 6 Soil physical properties used in the unsaturated zone.

In this case only numerical solutions are available, so this case was first simulated using MIKE SHE. These results are then compared with the coupled MIKE SHE- FEFLOW model in Figure 7. The comparison shows the results obtained from MIKE SHE (solid lines) with the coupled model (lines and symbols). Once again there is good agreement between the two models and the pressure distribution in the different layers is captured. Nevertheless there are some small differences in both the head elevations and timing close to the well. The simulated heads that are plotted for the coupled model are the FEFLOW model results interpolated to the MIKE SHE cell centres for each day. It should be noted that close to the well the gradients are quite large and the MIKE SHE grid resolution (10 m) is comparable to the distance to the 10 m well. This is the likely explanation for these small discrepancies.



(a) (b)

Figure 7 Comparison of the head elevation in 3 numerical different layers (Layer 1 top; Layer 3 middle; Layer5 bottom) simulated by MIKE SHE and by the Coupled (FEFLOW -MIKE SHE) model, respectively. The results are obtained at a point along the line through the pumping well, perpendicular to the river, (a) 10 m away from the well and (b) 50m away from the well.

4. DISCUSSION AND CONCLUSIONS

In this paper we develop and demonstrate a dynamic coupling of MIKE SHE and FEFLOW as an integrated modelling approach. This is achieved using the open modelling interface tools in OpenMI. The motivation for this study was to develop an integrated hydrological modelling tool that enhances the capabilities of both models. Firstly the powerful subsurface modelling capabilities of FEFLOW, especially grid refinement, three dimensional unsaturated flow and variable density flow including saltwater intrusion are made available to MIKE SHE. Conversely, the surface process capabilities in MIKE SHE particularly the ability to calculate dynamically recharge to groundwater directly from precipitation and potential evapotranspiration and subsequently to simulate groundwater –river exchanges are available to FEFLOW. Two test cases were presented representing transient stream depletion from groundwater drawdown. The first compared the coupled model in a simplified case corresponding to the analytical solution of Hunt (1999). The second case involving both transient saturated and unsaturated flow was compared to numerical simulations using MIKE SHE. . The tests were carried out as a verification of the coupling methodology and good matches with the analytical solution and MIKE SHE solutions were found.

The coupling developed here represents a challenging application of OpenMI technology. This coupling not only contains one-dimensional, two dimensional and three-dimensional elements but the coupling must also match the block-centred finite difference solutions from MIKE SHE with the variable mesh finite element solutions from FEFLOW. The exchange of data in both space and time exploits built-in tools available within the OpenMI framework. The initial results shown here verify the ability of the coupling between FEFLOW and MIKE SHE to represent dynamically the interactions between the river and groundwater systems in a few well-defined cases. The results also highlight the ability of the flexible finite element to represent effectively represent complex geometries and boundary conditions. Complementary investigations for lake-groundwater interaction have also been successfully carried out.

This new coupled tool provides the capability to address more complex integrated modelling problems which was one of the key motivations for developing OpenMI. We are currently investigating the use of this tool to examine problems related to saltwater intrusion. Here we can take full advantage of such a coupling by combining, the ability of MIKE SHE to represent spatial and temporal variations in recharge with the ability to represent variable density subsurface flow in FEFLOW. This will allow us not only to investigate more complex saltwater intrusion problems but also to examine, for example, the effects of climate changes on the management of coastal aquifers.

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